# Charge Density in Transition Metal Clusters: Supported vs Unsupported Metal-Metal Interactions 

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Experimental X-ray determination of the accurate electron density (ED) in compounds containing transition metals has grown as a major area in the past few years. Most of the progress is due to the recent availability of fast instrumentation like area-detectors (imaging plates ${ }^{1}$ or CCD cameras ${ }^{2}$ ) which provide full and very accurate datasets in short times also for large unit-cell crystals. The high sensitivity of CCD chips improves the overall quality of the measures, and the large redundancy of data collected allows a more accurate absorption correction, which further favors the study of polynuclear compounds even if they have low suitability factors. ${ }^{3}$ Until now, many experimental studies have been carried on metal dimers, and two recent works have examined the topological features of $\mathrm{M}-\mathrm{M}$ bonds in unsupported bimetallic compounds. ${ }^{2 a, 4}$ Few studies of trinuclear compounds are known in the literature, ${ }^{5}$ but these were undertaken when the quantum theory of atoms in molecules (QTAM) ${ }^{6}$ was not yet a common practice among experimentalists.

Here, we report the results of QTAM analysis on the experimental ED of a low nuclearity transition metal cluster. When this work was conceived, for the sake of simplicity "binary" metalcarbonyl clusters were scrutinized, but several difficulties were encountered. Finally, a $\mathrm{Co}_{4}(\mathrm{CO})_{12}$ derivative of pseudo $C_{s}$ symmetry, namely, $\mathrm{Co}_{4}(\mathrm{CO})_{8}\left(\mu_{2}-\mathrm{CO}\right)_{3} \mathrm{PPh}_{3}$ (1) (Figure 1), was chosen on the basis of the good quality of the crystals and the neutrality of the species. ${ }^{7}$

The most interesting features to investigate are the differences between the three unsupported and the three carbonyl-bridged $\mathrm{Co}-\mathrm{Co}$ bonds. According to conventional electron counting rules, both $\mathrm{Co}_{4}(\mathrm{CO})_{12}(2 \mathbf{a})$ and $\mathrm{Co}_{4}(\mathrm{CO})_{9}\left(\mu_{2}-\mathrm{CO}\right)_{3}(\mathbf{2 b})$ contain six metal-metal bonds; however, differences might arise in the QTAM view. In fact, while each unsupported $\mathrm{Co}-\mathrm{Co}$ interaction is associated with a bond path ( $b p$ ) and a bond critical point ( $b c p$ ), each $\operatorname{Co}\left(\mu_{2}-\mathrm{C}_{\mathrm{b}}\right) \mathrm{Co}$ moiety possesses only the $\mathrm{Co}-\mathrm{C}_{\mathrm{b}} b p$ s and $b c p s$ (Figure 1). All remaining $\mathrm{Co}-\mathrm{C}$ and $\mathrm{Co}-\mathrm{P}$ interactions have their $b p s$ and $b c p s^{8}$ as well as all intraligand bonds (Table 1); in addition, seven ring critical points ( $r c p$, one for each face of the tetrahedron ${ }^{9}$ and one for each phenyl group) and one cage critical

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Figure 1. Left: ORTEP view of $\mathrm{Co}_{4}(\mathrm{CO})_{11} \mathrm{PPh}_{3}$ (ellipsoids for nonhydrogen atoms are drawn at $50 \%$ probability); labels of C and H are omitted. Right: Scheme of the principal bond paths and $c p$ s found for $\mathbf{1}$.

Table 1. Averaged Results of the Topological Analysis on 1

|  | $(\AA(\AA)$ | $\rho\left(\mathbf{r}_{b c p}\right)$ <br> $\left(\mathrm{e}^{-3}\right)$ | $\nabla^{2} \rho\left(\mathbf{r}_{\text {bcp }}\right)$ <br> $\left(\mathrm{e} \AA^{-5}\right)$ | $H\left(\mathbf{r}_{\text {bcp }}\right)$ <br> $\left(\right.$ hartree $\left.\AA^{-3}\right)$ | $G\left(\mathbf{r}_{\text {bcp }}\right)^{a}$ <br> $\left(\right.$ hartree $\left.\AA^{-3}\right)$ |
| :--- | :--- | :--- | :---: | :--- | :--- |
| $\mathrm{C}-\mathrm{H}$ | $1.08(3)$ | $1.91(8)$ | $-16.4(1.5)$ | $-2.0(1)$ | $0.84(5)$ |
| $\mathrm{C}-\mathrm{C}$ | $1.397(4)$ | $2.11(3)$ | $-17.1(1.3)$ | $-2.32(1)$ | $1.12(1)$ |
| $\mathrm{P}-\mathrm{C}$ | $1.829(3)$ | $1.08(2)$ | $-5.5(4)$ | $-1.040(2)$ | $0.658(1)$ |
| $\mathrm{Co}_{2}-\mathrm{P}$ | $2.2418[3]^{b}$ | $0.505[5]^{b}$ | $2.52[1]^{b}$ | -0.199 | 0.375 |
| $\mathrm{O}_{\mathrm{t}}-\mathrm{C}_{\mathrm{t}}$ | $1.142(3)$ | $3.34(9)$ | $-4.6(11.3)^{c}$ | $-6.1(2)$ | $5.8(2)$ |
| $\mathrm{O}_{\mathrm{b}}-\mathrm{C}_{\mathrm{b}}$ | $1.167(2)$ | $3.14(4)$ | $-23.2(6.4)^{c}$ | $-5.9(4)$ | $4.3(2)$ |
| $\mathrm{Co}_{\text {bas }}-\mathrm{Co}_{4}$ | $2.528(8)$ | $0.252(3)$ | $1.81(6)$ | $-0.039(1)$ | $0.166(1)$ |
| $\mathrm{Co}^{-\mathrm{C}_{\mathrm{t}}}$ | $1.80(2)$ | $1.00(3)$ | $11.5(6)$ | $-0.540(1)$ | $1.344(5)$ |
| $\mathrm{Co}_{1,3}-\mathrm{C}_{3,5}$ | $1.974(3)$ | $0.67(4)$ | $6.3(1)$ | $-0.27(4)$ | $0.71(4)$ |
| $\mathrm{Co}_{2}-\mathrm{C}_{3,5}$ | $1.91(1)$ | $0.73(1)$ | $8.1(1)$ | $-0.29(1)$ | $0.858(7)$ |
| $\mathrm{Co}_{1,3}-\mathrm{C}_{8}$ | $1.94(1)$ | $0.76(1)$ | $7.7(3)$ | $-0.328(8)$ | $0.865(3)$ |

${ }^{a} G\left(\mathbf{r}_{\mathrm{bcp}}\right)$ is calculated according to Abramov, Y. A. Acta Crystallogr. 1997, A53, 264; for $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{H}$ Bonds, $G\left(\mathbf{r}_{\mathrm{rcp}}\right)$ was estimated adopting the partitioning of sp 2 carbons. Standard deviations from the mean are reported in parenthesis. $\mathrm{C}_{\mathrm{t}}, \mathrm{O}_{\mathrm{t}}=$ terminal $\mathrm{C}, \mathrm{O} ; \mathrm{C}_{\mathrm{b}}, \mathrm{O}_{\mathrm{b}}=$ bridging C,O; $\mathrm{Co}_{\text {bas }}=\mathrm{Co} 1, \mathrm{Co} 2, \mathrm{Co} 3{ }^{b}$ Standard uncertainty. ${ }^{c}$ The large spread of this value (here accounted by the huge deviation from the mean) is due to the $\mathrm{C}-\mathrm{O} b c p$ lying very close to the nodal surface of the Laplacian. ${ }^{2 a, b}$
point (сср, inside the tetrahedron) are found as required by the Poincaré-Hopf rule. ${ }^{10}$

Given the observed behavior, a question which might arise as to whether the absence of $\mathrm{M}-\mathrm{M}$ bond path in the basal plane is due to some bias, possibly related to the short distance between the "missing" $\mathrm{M}-\mathrm{M} b c p$ and the bridging atom, or it is inherent

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Figure 2. $\rho(\mathbf{r})$ for 1, 2a, and $\mathbf{2 b}$ along the line bisecting $\mathrm{Co} 1-\mathrm{Co} 2-$ Co 3 angle and normal to $\mathrm{Co} 1-\mathrm{Co3}$ ( $x$ is the distance from Co 2 ). The minimum at $x \approx 1.5 \AA$ corresponds to the $r c p$ in the basal plane. The maximum at $x \approx 2.3 \AA$ for $2 \mathbf{a}$ indicates the presence of $\mathrm{Co} 1-\mathrm{Co3} b p$, while in the two bridged systems the charge is spread out and the Co Co $b p$ disappears.
to supported interactions. A plot along the line bisecting the $\mathrm{Co} 1-$ $\mathrm{Co} 2-\mathrm{Co} 3$ angle (and directed perpendicular to $\mathrm{Co} 1-\mathrm{Co} 3$ edge) does clarify the behavior of the electron density (see Figure 2): $\rho(\mathbf{r})$, after the minimum (which corresponds to the $r c p$ ), rises monotonically toward the carbon and no $\mathrm{M}-\mathrm{M} b c p$ (i.e., a maximum) is found. Ab initio EDs, calculated for 2a and $\mathbf{2 b},{ }^{11}$ allow visualization of what happens in the re-organization of terminal into bridging ligands. Indeed, given the $\rho(\mathbf{r})$ cuts computed along the same direction, it is clear that, upon bridging, the $\mathrm{M}-\mathrm{M}$ density has been spread out (and not just overwhelmed by the carbon density). Judging from the curvature of the two profiles, ${ }^{12}$ charge reorganization is somewhat more "complete" in the experimental than the theoretical model, but the relevant feature here is the difference between the two theoretical shapes.

Thus, according to QTAM, there are no direct metal-metal bonds in the basal plane, and the bridging carbonyls apparently bind at their expense. The current explanation for such behavior stands on the concept of multicenter delocalized bonding; ${ }^{13}$ in fact, each $\operatorname{Co}\left(\mu_{2}-\mathrm{C}_{\mathrm{b}}\right) \operatorname{Co}$ moiety can be seen as a three-center-four-electron bond. This is augmented by the consideration that the stereochemical changes occurring upon transformation from terminal to bridging carbonyls reorient the directions of maximum bonding (of the pseudo-octahedral metal fragment): that is, the metal orbital involved in the $\mathrm{M}-\mathrm{M}$ bond in $\mathbf{2 a}$, is directed toward $\mathrm{C}_{\mathrm{b}}$ in $\mathbf{2 b}$ and $\mathbf{1}$ (see the $\mathrm{Co}-\mathrm{C}_{\mathrm{b}} b p$ in Figure 3). Having this in mind, we can argue that also in bridged metal dimers, where no $b p s$ were found, ${ }^{14} \mathrm{M}-\mathrm{M}$ bonding is no longer "direct", but rather "indirect" because it is obtained through a third part (i.e., the carbonyl).

How can we distinguish a delocalized three-center ( $\mathrm{M}-\mathrm{C}-$ $\mathrm{M})$ bond from a couple of localized two-center $(\mathrm{M}-\mathrm{C})$ interactions? If a comparison with a ketonic carbonyl $\mathrm{RC}(\mathrm{O}) \mathrm{R}$ is worthwhile, the $\mathrm{Co}\left(\mu_{2}-\mathrm{CO}\right)$ Co moiety has structural differences such as a shorter $\mathrm{C}-\mathrm{O}$ distance, a smaller $\mathrm{R}-\mathrm{C}-\mathrm{R}$ angle, and a "shorter" $\mathrm{R} \cdots \mathrm{R}$ contact, ${ }^{15}$ all due to an "incomplete" $\mathrm{sp} \rightarrow \mathrm{sp}^{2}$ rehybridization of the carbon. At the QTAM level one may add that the ketonic carbon has two valence shell charge concentrations

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Figure 3. The Laplacian distribution for a bridging carbonyl (left) and the three terminal carbonyl types (right) in $\mathbf{1}$; negative contours are solid lines, the superimposed bold lines represent the bond paths. Note the small $\mathrm{Co} 1-\mathrm{C} 8-\mathrm{Co} 3 b p$ angle and the large charge concentration on C 8 . C 1 , which is bonded in an "equatorial" site, shows a perturbation of $\nabla^{2} \rho(\mathbf{r})$ toward the apical metal (Co4), a feature which is not observed for "axial" (C2) and "apical" (C11) carbonyls (which lie farther from vicinal metals).
(VSCC), ${ }^{16}$ directed toward the R groups, while in $\operatorname{Co}\left(\mu_{2}-\mathrm{CO}\right)$ Co only one, bisecting the $\mathrm{Co}-\mathrm{C}_{\mathrm{b}}-\mathrm{Co}$ angle, is found. ${ }^{17}$ This suggests that two separated $\mathrm{Co}-\mathrm{C}$ bonded electrons cannot be localized on each carbon (in agreement, a natural bond orbital analysis on $\mathbf{2 b}$ wave function does not allocate a proper orbital for each $\mathrm{Co}-\mathrm{C}_{\mathrm{b}}$ bond). The two $\mathrm{Co}-\mathrm{C}_{\mathrm{b}} b p$ lines are quite straight as a result of the presence of both a "central" $\sigma$-donation and a lateral $\pi$-back-donation, but they are markedly curved at $\mathrm{C}_{\mathrm{b}}$; as a result the $\mathrm{Co}-\mathrm{C}_{\mathrm{b}}-\mathrm{Co} b p$ angle ${ }^{18}$ is $18(4)^{\circ}$ smaller than the geometrical one (see Figure 3), in agreement with the hypothesis that donation occurs through the CO $5 \sigma$ orbital. ${ }^{13 a}$


Some other results of QTAM analysis are worth noting (see Table 1). The density at the $\mathrm{Co}-\mathrm{C}_{\mathrm{b}} b c p$ is more than half the density of $\mathrm{Co}-\mathrm{C}_{\mathrm{t}}$ bonds, which is an additional proof of the $\rho(\mathbf{r})$ redistribution toward the bridging carbonyls. If compared to $\mathrm{C}_{\mathrm{t}}-$ $\mathrm{O}_{\mathrm{t}}, \mathrm{C}_{\mathrm{b}}-\mathrm{O}_{\mathrm{b}}$ has a larger internuclear distance, a reduced bond order (i.e., less density at the $b c p$ ), and less polarity (the ratio between the kinetic energy density $\mathrm{G}(\mathbf{r})$ and $\rho(\mathbf{r})$ at $b c p$ is smaller and the carbon basin is larger). The three $\mathrm{Co}_{\text {bas }}-\mathrm{Co}_{4}$ bonds show features similar to those of $\mathrm{M}-\mathrm{M}$ bonds in unsupported dimers (at the $b c p, \rho(\mathbf{r})$ is small, the Laplacian $\nabla^{2} \rho(\mathbf{r})$ is positive, the total energy density $H(\mathbf{r})$ is negative, and $G(\mathbf{r}) / \rho(\mathbf{r})<1)$. ${ }^{2 \mathrm{a}}$

With this experimental work, we have shown that QTAM, at variance from deformation density maps, sheds light on the differences between supported and unsupported $\mathrm{M}-\mathrm{M}$ interactions, confirming that the $\mathrm{M}-\mathrm{C}-\mathrm{M}$ bond is a delocalized threecenter interaction and that $\mathrm{M}-\mathrm{M}$ bonding is indirect because it is achieved through the carbonyl. Moreover, it may be worth noting that $\mathrm{Co}_{4}(\mathrm{CO})_{11} \mathrm{PPh}_{3}$ is one of the larger (and less suitable) ${ }^{3}$ molecules studied until now with this technique; nevertheless, the internal (with respect to the $C_{s}$ pseudo-symmetry) and external (with respect to theoretical computations) coherence of the derived parameters is qualitatively good, thus suggesting that the experimental limit is still to be reached. For these reasons, we are now planning a study on octahedral clusters containing the $\mathrm{Co}_{3}\left(\mu_{3^{-}}\right.$ CO) moiety, not yet characterized even theoretically.

Supporting Information Available: Tables detailing the experimental and theoretical results (PDF). This material is available free of charge via the Internet at http://pubs.acs.org.
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[^0]:    ${ }^{\dagger}$ DCSSI and CNR-CSMTBO.
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    (2) (a) Macchi, P.; Proserpio, D. M.; Sironi, A. J. Am. Chem. Soc. 1998, 120, 13429 and references there reported in note 19. (b) Abramov, Y.; Brammer, L.; Klooster, W. T.; Bullock, R. M. Inorg. Chem. 1998, 37, 6317. (c) Scherer, W.; Hieringer, W.; Spiegel, M.; Sirsch, P.; McGrady, G. S.; Downs, A. J.; Haaland, A.; Pedersen, B. Chem. Commun. 1998, 2471.
    (3) According to (a) Coppens, P. Isr. J. Chem. 1977, 16, 144 and (b) Feil, D. ibid. 149, the ratio $S=V / \Sigma_{j}\left[n_{j}\right]^{2}\left(V=\right.$ cell volume, $n_{j}=$ number of core electrons for $j$-th atom) indicates the suitability of ED studies (the higher $S$ is, the better the system is). Transition metal compounds have small $S(<0.6)$, and for $1 S=0.49$.
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    (6) Bader, R. F. W. Atoms in Molecules: a quantum theory; International series of monographs on chemistry 22; Clarendon Press: Oxford, 1990.

[^1]:    (7) Homonuclear clusters (like $\mathrm{Co}_{4}(\mathrm{CO})_{12}$ ) have disordered structures; other species (like $\left[\mathrm{FeCo}_{3}(\mathrm{CO})_{12}\right]^{-}$) always presented disorder of the metal cage or reduced scattering despite several trials with different cations. 1 was synthesized as reported by: (a) Cetini, G.; Gambino, O.; Rossetti, R.; Stanghellini, P. L. Inorg. Chem. 1968, 7, 609 and (b) Darensbourg, D. J.; Incorvia, M. J. Inorg. Chem. 1980, 19, 2585. The X-ray structure was originally reported in: (c) Darensbourg, D. J.; Incorvia, M. J. Inorg. Chem., 1981, 20, 1911. Crystals were obtained by slowly cooling at low temperature a saturated $n$-hexane solution. Crystal data: $a=11.748(1) \AA, b=16.898(2) \AA, c=$ 15.289(1) $\AA, \beta=100.42(3)^{\circ}, V=2985 \AA^{3}$, monoclinic, $P 2_{1} / n, Z=4.155163$ reflections (31 404 independent, $R_{\text {int }}=\Sigma\left|F_{0}^{2}-F_{\text {mean }} 2\right| / \Sigma F_{\mathrm{o}}^{2}=0.0290$ ) were collected at $T=120 \mathrm{~K}$ on a SMART CCD area-detector diffractometer, $\lambda=$ $0.71073 \AA\left(\sin \theta_{\text {max }} / \lambda=1.10 \AA^{-1}\right)$; experimental conditions were similar to those reported in ref 2a. The multipolar model ((d) Hansen, K. H.; Coppens, P. Acta Crystallogr. 1978, A34, 909. (e) Stewart, R. F. Acta Crystallogr. 1976, A32, 565) implemented in software XD ((f) Koritsanszky, T.; Howard, S. T.; Su, Z.; Mallinson, P. R.; Richter, T.; Hansen, N. K. XD, Computer Program Package for Multipole refinement and Analysis of Electron Densities from Diffraction Data; Free University of Berlin: Germany, June, 1997) was used to refine the aspherical density, expanding Co and P up to hexadecapoles, C and O up to octupoles, and H up to dipoles. The final agreement indexes were $R 1=\Sigma| | F_{\mathrm{o}}\left|-\left|F_{\mathrm{c}}\right|\right| / \Sigma\left|F_{\mathrm{o}}\right|=0.0190$ and wR2 $=\left(\Sigma\left(F_{\mathrm{o}}^{2}-F_{\mathrm{c}}^{2}\right)^{2} / \Sigma w F_{\mathrm{o}}^{4}\right)^{1 / 2}$ $=0.0239$, for the 23523 unique reflections with $I>2 \sigma(I)$.
    (8) The terminal CO and the phosphyne ligand show good agreement with those of ref 2 b .
    (9) The basal plane is a six-atom ring $\left(\mathrm{Co}_{3} \mathrm{C}_{3}\right)$, while the three lateral faces are four-atom rings $\left(\mathrm{Co}_{3} \mathrm{C}\right)$.
    (10) Collard, K.; Hall, G. G. Int. J. Quantum Chem. 1977, 12, 623.

[^2]:    (11) $\mathrm{HF} / 6-311++\mathrm{G}^{* *}$ calculation were carried on the hypothetical $T_{d}$ stereochemistry of $\mathbf{2 a}$ and the experimentally known $C_{3 v}$ geometry of $\mathbf{2 b}$ with GAUSSIAN94 packadge (Frisch, M. J.; Trucks, G. W.; Schlegel, H. B.; Gill, P. M. W.; Johnson, B. G.; Robb, M. A.; Cheeseman, J. R.; Keith, T.; Petersson, G. A.; Montgomery, J. A.; Raghavachari, K.; Al-Laham, M. A.; Zakrzewski, V. G.; Ortiz, J. V.; Foresman, J. B.; Peng, C. Y.; Ayala, P. Y.; Chen, W.; Wong, M. W.; Andres, J. L.; Replogle, E. S.; Gomperts, R.; Martin, R. L.; Fox, D. J.; Binkley, J. S.; Defrees, D. J.; Baker, J.; Stewart, J. P.; HeadGordon, M.; Gonzalez, C.; Pople, J. A. Gaussian, Inc.: Pittsburgh, PA, 1995); all $\mathbf{C o}-\mathrm{Co}$ distances were kept at the values observed for $\mathbf{2 b}$.
    (12) The presence of an almost degenerate critical point (i.e., with rank $<3$ ), is related to that of a catastrophe point in the structure space (ref 6, Chapter 3), that is, a structural instability or an easy $C_{3 v} \leftrightarrow T_{d}$ interconversion.
    (13) (a) Kostic, M. N.; Fenske, R. F. Inorg. Chem. 1983, 22, 666. (b) Benard, M. Inorg. Chem. 1979, 18, 2782. (c) Heijser, W.; Baerends, E. J.; Ros, P. Discuss. Faraday Soc. (Symp.) 1980, 14, 211.
    (14) (a) Low, A. A.; Kunze, K. L.; MacDougall, P. J.; Hall, M. B. Inorg. Chem. 1991, 30, 1079. (b) Bo, C.; Sarasa, J. P.; Poblet, J. M. J. Phys. Chem. 1993, 97, 6362 .
    (15) Which apparently suggests a comparison with cyclopropanone rather than with a generic keton.

[^3]:    (16) According to Bader (see ref 6, chapter 7) a VSCC is a maximum of $L(\mathbf{r})=-\nabla^{2} \rho(\mathbf{r})$ in the valence region and can be associated to bonded electrons within Lewis formalism.
    (17) In 1, one of the three bridging carbonyls actually shows two (very close) VSCCs toward the metals, while the other two $\mathrm{C}_{\mathrm{b}}$ have only one in agreement with the theoretical results on 2b (see also ref 14b).
    (18) Averaged over the three independent bridges; the theoretical value is $27^{\circ}$

